

# Work – Energy Theorem

1. Explain how (+) and (-) work applies to the work – energy theorem.

$+W \Rightarrow$  increasing energy

$-W \Rightarrow$  decreasing energy

2. A 50.0 kg sled is sitting still on a flat snowy field. you grab the rope attached to the sled and pull with a constant 50.0 N force directed at  $60.0^\circ$  above horizontal for 20.0 meters. The force of friction acting on the sled is 20.0N.

a) How much work did you do pulling the sled?

$$W = Fd \cos \theta = 50\text{N}(20\text{m}) \cos 60^\circ$$

$$W_{\text{you}} = \underline{5.00 \times 10^2} \text{ J}$$

B) How much work was done by friction?

$$W = Fd \cos \theta = 20\text{N}(20\text{m}) \cos 180^\circ$$

$$W_f = \underline{-4.00 \times 10^2} \text{ J}$$

c) What was the net work done on the sled?

$$W_{\text{net}} = W_{\text{you}} + W_f$$

$$W_{\text{NET}} = \underline{1.00 \times 10^2} \text{ J}$$

d) What was the final  $E_k$  of the sled?

$$W_{\text{net}} = \Delta E_k = E_{kf} - E_{ki} \rightarrow 0$$

$$E_k = \underline{1.00 \times 10^2} \text{ J}$$

e) What is the final velocity of the sled?

$$\Sigma u = \frac{1}{2}mv^2$$

$$V_f = \underline{2.00} \text{ m/s}$$

3. Kenny (60.0kg) snowboards over the crest of a hill at 3.00m/s. He goes straight down slope a distance of 50.0m and hits a tree moving at 18.0m/s (that's Kenny moving at 18m/s, not the tree). The force of friction acting on Kenny's board was 75.0N. Calculate:

a) Kenny's initial KE at the top of the hill.

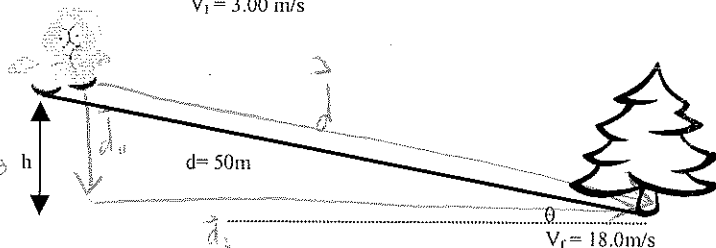
$$\Sigma u = \frac{1}{2}mv_i^2$$

$$KE_i = \underline{2.70 \times 10^2} \text{ J}$$

b) Kenny's final KE just before hitting the tree.

$$\Sigma u = \frac{1}{2}mv_f^2$$

$$V_i = 3.00 \text{ m/s}$$



$$KE_f = \underline{9720} \text{ J}$$

c) The net work done on Kenny (before he hits the tree)

$$W_{\text{net}} = \Delta \Sigma u$$

$$W_{\text{NET}} = \underline{9450} \text{ J}$$

d) The work done on Kenny by friction.

$$W_f = Fd \cos \theta = 75\text{N}(50\text{m}) \cos 180^\circ$$

$$W_f = \underline{-3750} \text{ J}$$

e) The work done on Kenny by gravity.

$$W_{\text{net}} = W_g + W_f$$

$$W_g = \underline{13200} \text{ J}$$

f) Find the height of the hill

$$W_g = F_g d_{\parallel} = mgh; \quad (d_{\parallel} = h)$$

$$h = \underline{22.4} \text{ m}$$

g) Find  $\theta$ .

$$\sin \theta = \frac{h}{d}$$

$$\theta = \underline{26.7}^\circ$$

$$\theta = \sin^{-1}\left(\frac{h}{d}\right)$$